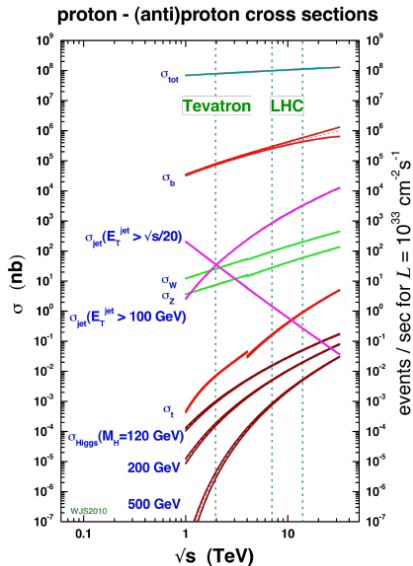


## Lecture 23: Hadron Collider Physics (II)

Nov 15, 2015

Include slides on Top taken from  
Gianluca Petrillo's talk at Moriond 2013

# Reminder: Cross Sections at Hadron Colliders

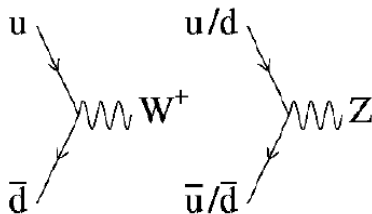


- Rates determined by
  - ▶ Hard Scattering Cross Section
  - ▶ Parton luminosity
- QCD processes dominate
  - ▶ EW rates lower by  $\alpha/\alpha_S$
- Main background for  $W$  and  $Z$  production: QCD jets
- Almost impossible to see single  $W \rightarrow q\bar{q}'$  or  $Z \rightarrow q\bar{q}$  above jet background
  - ▶ UA2 managed to do this with special trigger and very large background
  - ▶ But almost all studies of  $W$  and  $Z$  in hadron colliders in leptonic decay modes

$$W^\pm \rightarrow \begin{matrix} \ell^- \nu_\ell \\ \ell^+ \bar{\nu}_\ell \end{matrix}$$

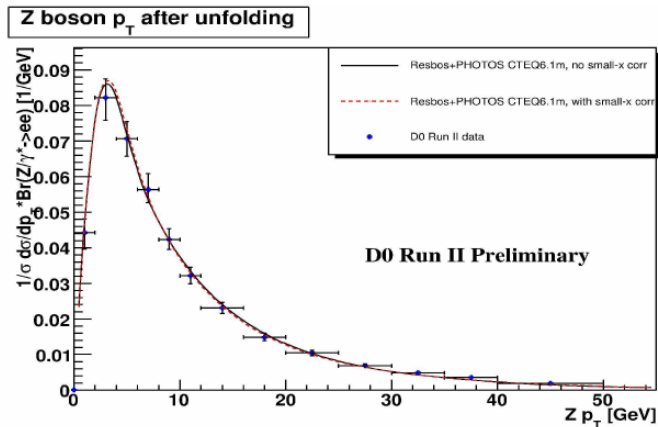
$$Z \rightarrow \ell^+ \ell^-$$

# Production of $W$ and $Z$ Bosons



- Lowest order diagram: quark annihilation
- At lowest order,  $W$  and  $Z$  are produced with no  $p_T$

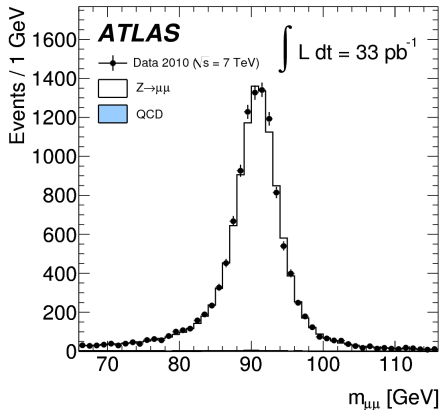
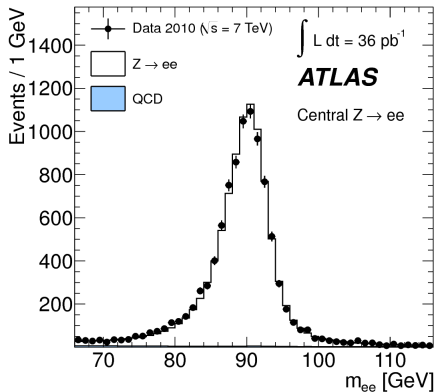
# Full QCD Calculation: Boson $p_T$ Remains Small



Distribution dominated by multiple soft gluon emission

# Reconstruction of $Z$ Bosons

- In general, limited to leptonic modes
  - ▶ Large QCD jet background swamps signal in jet channel
  - ▶ In principle, can find regions of phase space where hadronic mode can be reconstructed, but in very specialized analyses with other objects
  - ▶ Two high  $p_T$  leptons, nearly back-to-back
  - ▶ Reconstruction straightforward, background small



# Reconstruction of $W$ Bosons

- Again, restricted to lepton channels
- But here, one of the nearly back-to-back leptons is a neutrino

How do we “detect” a particle that doesn't interact in our detector?

- Look for momentum imbalance and assign the missing momentum to the  $\nu$

But in hadron colliders, limited to using only the 2 transverse components of the momentum

# Neutrino Reconstruction

- Must add the momentum of all objects in the event
- The traditional way: calorimeter only



Calorimeter “Tower”

detector

Define  $\vec{E}_T$  (2 vector)

$$\begin{aligned}\vec{E}_T &= -\sum_{\text{Towers}} E_{iT} \hat{n}_i \\ &= -\sum E_i \sin \theta_i \hat{n}_i\end{aligned}$$

Similarly total  $E_t$

$$\begin{aligned}E_t &= \sum_{\text{Towers}} |E_{iT}| \\ &= \sum |E_i| \sin \theta_i\end{aligned}$$

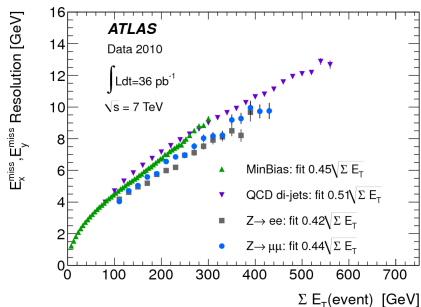
- ▶ Create a grid of calorimeter towers
- ▶ Treat each tower as a massless particle with momentum direction normal to the tower
- For better resolution: Use reconstructed objects
  - ▶ Combine the momentum of all the jets and electrons, muons
  - ▶ Then add the remaining unused energy using towers as above
  - ▶ When combining, can have different calibrations to each object

# A Comment on Resolution

- Calorimeter resolution depends on energy deposited

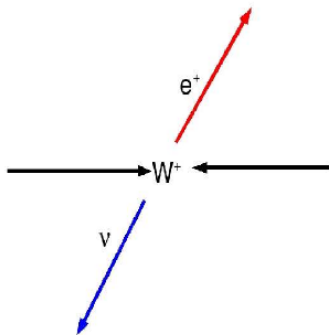
$$\sigma/E_T \propto \sqrt{\sum E_T}$$

- Measurement is also sensitive to detector cracks and noise
- Degrades with pileup





# W Decay: Lepton $p_T$ Distribution



- In CM frame,  $e$  and  $\nu$  are back-to-back and balance  $p_T$ :

$$p_T^2 = \frac{1}{4} \hat{s} \sin^2 \theta$$

- Changing variables from  $\cos \theta$  to  $p_T$  introduces a Jacobian:

$$\frac{d \cos \theta}{dp_T^2} = -\frac{2}{\hat{s} \cos \theta}$$

- But we know

$$\frac{d\sigma}{d \cos \theta} \propto (1 + \cos^2 \theta)$$

so

$$\frac{d\sigma}{dp_T^2} \propto \frac{(1 + \cos^2 \theta)}{\hat{s} \cos \theta} \propto \frac{2 (1 - 2p_T^2/\hat{s})}{\hat{s} (1 - 4p_T^2/\hat{s})^{\frac{1}{2}}}$$

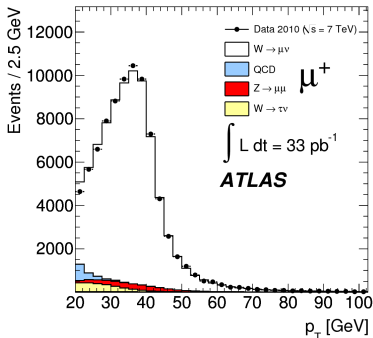
# The Jacobean Peak

- Notice

$$\frac{d\sigma}{dp_T} \propto \frac{1 + \cos^2 \theta}{\cos \theta}$$

Diverges for  $\theta = \pi/2$  (which is  $p_T = \sqrt{\hat{s}}/2$ )

- Divergence results from the Jacobean factor in transformation to  $p_T$
- Integration over Breit-Wigner removes singularity but leaves the peak
- HO corrections give  $W$  transverse momentum and further smear the peak



# Transverse Mass

- $W$   $p_T$  gives  $\ell$  and  $\nu$  by same boost
- Define  $\ell$ - $\nu$  transverse mass:

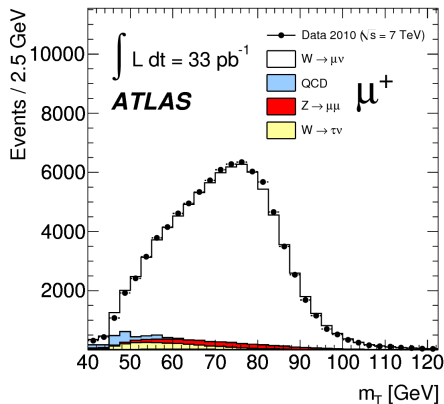
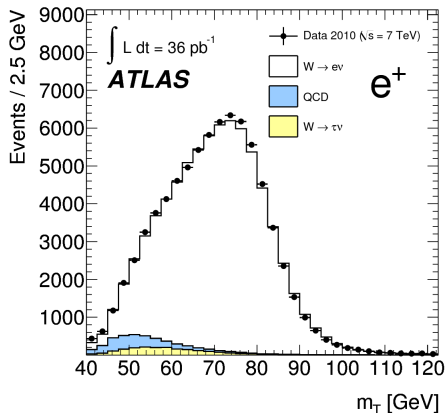
$$m_T^2 = (E_T^\ell + E_T^\nu)^2 - (\vec{p}_T^\ell + \vec{p}_T^\nu)^2$$

- Note that for  $p_T^W = 0$ ,  $m_T = 2|p_T^\ell| = 2|p_T^\nu|$
- Thus

$$\frac{d\sigma}{dm_T^2} = 4 \frac{d\sigma}{dp_T^2}$$

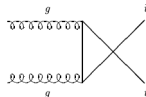
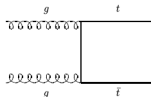
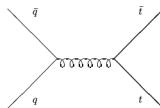
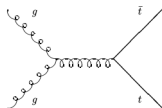
- $m_T$  sensitive to transverse boosts only at second order
  - ▶ Predicted  $m_T$  distribution not very sensitive to modeling of boson  $p_T$
- But  $m_T$  more sensitive to detector resolution since depends on measurement of the  $\nu$

# Transverse Mass for $W$ Bosons



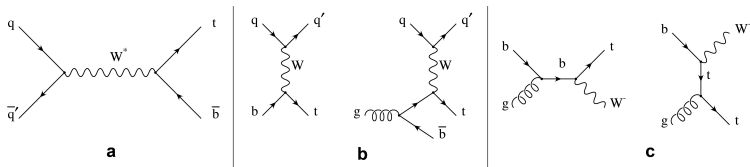
- Background small in both  $e$  and  $\mu$  channels
- Small theoretical uncertainties: a better choice of variable than lepton  $p_T$  in most cases

# Top-Pair Production



- Strong production:  $t\bar{t}$  pairs
- Tevatron: ( $p\bar{p}$  collider)
  - ▶ Production rate suppressed:  $2m_{top} \sim 0.2\sqrt{s}$
  - ▶ 15%  $gg$ , 85%  $q\bar{q}$
- LHC: ( $pp$  collider)
  - ▶ Production rate larger  $2m_{top} \sim 0.05\sqrt{s}$
  - ▶ 90%  $gg$ , 10%  $q\bar{q}$

# Single Top Production Through EW Processes

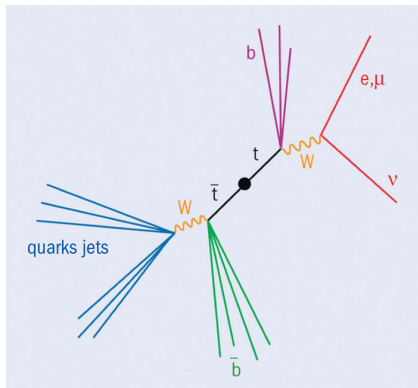
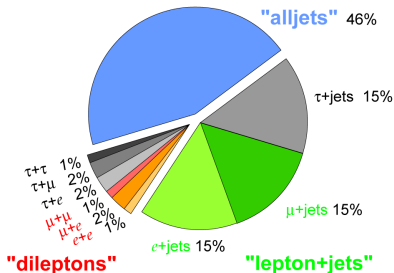


- Characterize as “s-channel”, “t-channel”, “ $W + t$ ”
- t-channel is the largest contribution, s-channel the smallest
- More difficult to isolate than the strong pair production
- Will concentrate on  $t\bar{t}$  production for most of today, but will return to this process towards the end of the lecture

# Top Decay Signatures ( $t\bar{t}$ Production)

- $t \rightarrow Wb$  BR  $\sim 100\%$  in SM ( $V_{tb}$ )
- Top lifetime  $\sim 5 \times 10^{-25}$  sec  
Decays before hadronization
- Top Pair production gives:

Top Pair Branching Fractions



# Top Reconstruction: The Basics

- Top pairs yield 6 high  $p_T$  objects
- Separate search strategies for dilepton, single lepton and all hadronic channels
  - ▶ Dilepton clean, but  $2\nu$ 's so full mass reconstruction not possible
  - ▶ Single lepton: Good S:B. The golden channel
  - ▶ All-hadronic: Must separate from very large QCD multijet background: possible with  $b$ -tagging, but difficult to get a pure signal

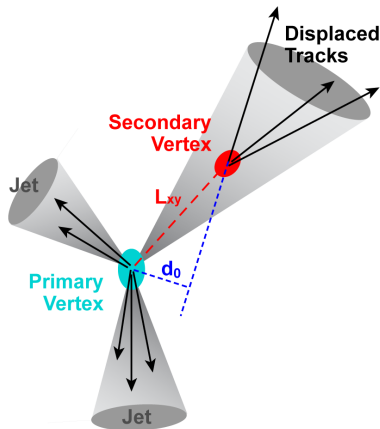


# Top Analysis Strategy

- Goal: Maximize top signal while reducing QCD background
- Top decay products central and at high  $p_T$ 
  - ▶ Typical Tevatron cuts:  $p_T > 15 \text{ GeV}$
  - ▶ Typical LHC cuts:  $p_T > 25 \text{ GeV}$
- Di- and single lepton channels have missing  $E_T$ 
  - ▶ Define  $H_T = \sum_i E_T$  where sum is over reconstructed objects
- Two  $b$ -jets in final state: identification of  $b$ 's greatly reduced background rate

# Jets Produced from $b$ -quarks

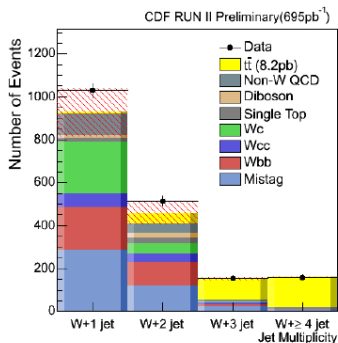
- Characteristics of  $B$  decays':
  - ▶  $B$  lifetime long
  - ▶ Semileptonic BR 10% per species
- Two methods of  $b$ -tagging
  - ▶ Displaced vertex tag
  - ▶ "Soft" leptons inside jets
- Today, multivariate techniques combine all information into a single metric



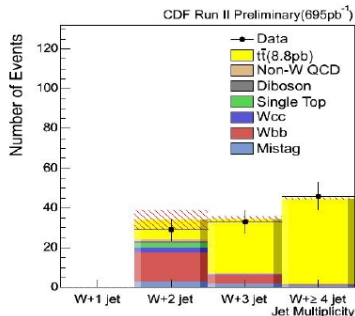
# Reconstructing Top in Single Lepton Channel

- Sample contains lepton, missing energy and  $\geq 4$  jets  
(additional jets from initial or final state radiation)
  - ▶ 2 jets reconstruct to  $W$  mass
  - ▶  $\ell + \nu$  reconstruct to  $W$  mass  
(must use transverse mass since  $p_z^\nu$  not measured)
  - ▶ 2 jets are  $b$ -jets
  - ▶ Each  $W + b$  reconstructs to a top
- Many possible combinations of objects possible
  - ▶ Can apply constraints to pick the best combinatorial choice
  - ▶ Or can use all choices, weighting with probability
- Signal can be observed without  $b$ -tagging if high  $H_T$  cut applied
- But  $b$ -tagging reduces combinatorial background

With b-tagging, Top dominated sample was selected at the Tevatron

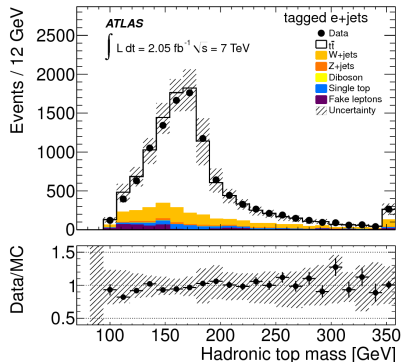
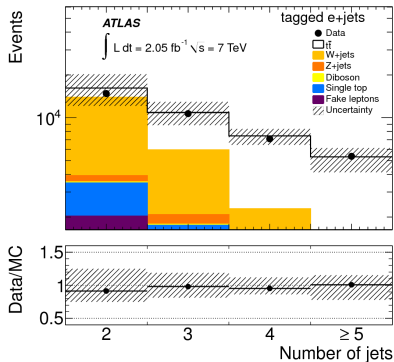


Single b-tag and HT>200 GeV



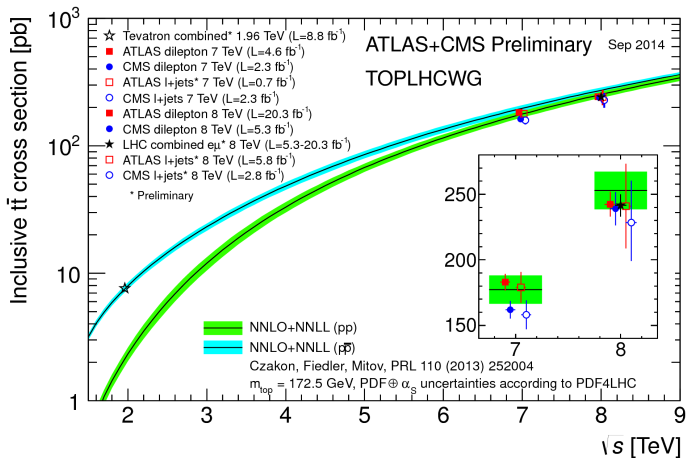
Double Tag

# At LHC, large, clean samples available



- Above require single b-tagged jet
- Right hand plot after kinematic likelihood fit and requirement of at least 4 jets

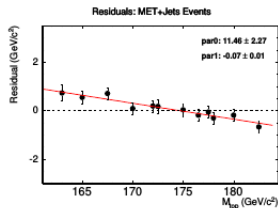
# Top Pair Cross Section



- Good agreement with pQCD predictions
- Important since top a major background to BSM searches

The measurements of top mass goes through some common steps:

- 1 assign a **likelihood** for each event, function of the top mass:  $L_i(m_t; \dots)$
- 2 **maximize** a global likelihood  $L(m_t; \dots) = \prod_{i \in \text{events}} L_i(m_t; \dots)$ , including all the events, to extract the  $m_t$  estimator
- 3 **calibrate** to remove any bias of the method



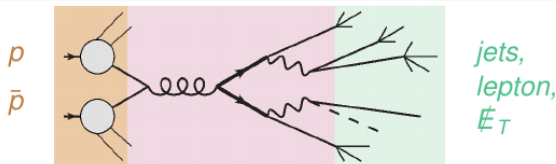
Calibration curve of  $m_t$  from CDF  
measurement from  $8.7 \text{ fb}^{-1}$  in  $\cancel{E}_T + \text{jets}$

- our analyses are calibrated on Monte Carlo simulation
- ⇒ we measure  $m_t$  with the definition implemented in MC!
- the precision of the experimental measurements helps the *interpretation* of this parameter (cfr. [PRD 80, 071102 \(2009\)](#))

Matrix Element method exploits the **full topology of the event**:

$$P(x, m_t) = \frac{1}{\sigma(m_t)} \int \sum_{\text{flavours}} f(q_1) f(q_2) \sigma(y, m_t) \mathcal{W}(x, y) dq_1 dq_2 dy$$

*scattering matrix element* (in  $\sigma$ ) for a final-state parton configuration “y” (including 4-momenta of all the 6 final state particles)



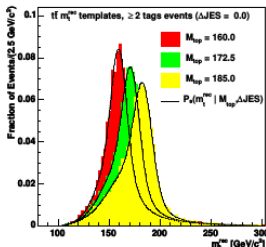
probability  $f(q_{1/2})$  of having a specific initial state (*Parton Distribution Functions*)

probability  $\mathcal{W}$  of reconstructing the scattering final state “y” as our measured jets/lepton objects “x” (*Transfer Functions*)

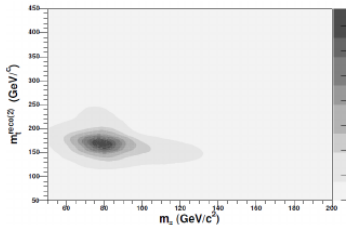


Templates method interprets the distribution of **one or more observables** sensitive to  $m_t$  as probability densities:

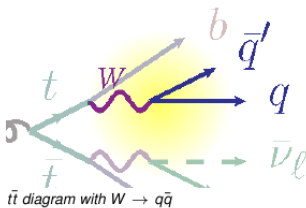
- distributions are **extracted from full detector simulation**
- **correlations** between observables *can* be included
- up to three observables used



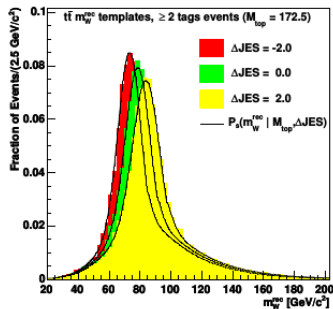
$m_t$  template (CDF measurement from  $5.8 \text{ fb}^{-1}$  in all-hadronic final state)



$m_t$  vs.  $m_{ij}$  template ( $m_t=171.5 \text{ GeV}/c^2$ ) from CDF measurement from  $8.7 \text{ fb}^{-1}$  in  $\ell$ +jets



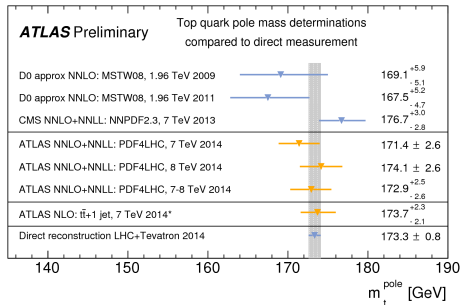
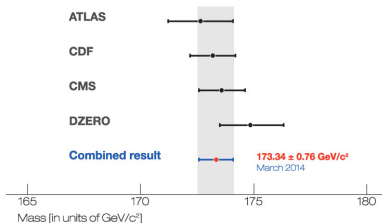
- in some final states,  $W$  boson can be *fully reconstructed*
- $\Rightarrow$  constrain a  $m_W$  estimator with the known  $W$  mass
- “nuisance parameter”  $\Delta_{JES}$  is measured, describing an additional **global scale** of jet energy



$m_{jj}$  template (CDF measurement from  $5.8 \text{ fb}^{-1}$  in all-hadronic final state,  $m_t = 172.5 \text{ GeV}/c^2$ ) =

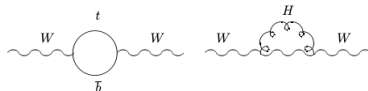
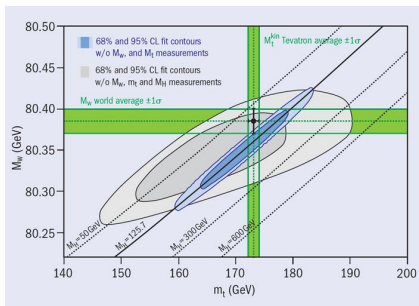
# Top Mass Measurement Summary

## Top quark mass measurements



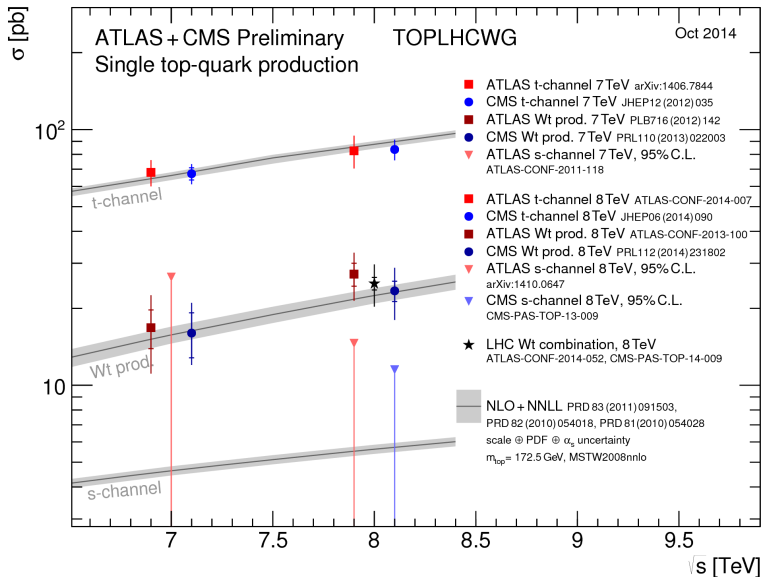
- Good agreement between experiments for direct measurement of  $m_{top}$
- $m_{top}$  derived from cross section consistent with direct measurements

# Why does $m_{top}$ matter?



- $m_W$  depends quadratically on  $m_{top}$  and logarithmically on  $m_{Higgs}$
- Would also be sensitive to other BSM particles with moderate mass
- Before Higgs discovered, gave prediction for its mass
- Now, can constrain possible BSM physics

# Single Top Production



# Using Top to Search for New Physics

